

# Rectangle Tangle

The rectangle was divided into lots of shapes.

I focused on each alone.

$\frac{1}{8} \leftarrow$  Shape 1: Shape 1 was  $\frac{1}{8}$  because

Answer

$\frac{1}{8}$

the big rectangle was divided into four main quarters. The shape was one half of the quarters which means  $\frac{1}{4} \div 2 = \frac{1}{8}$ . You can make  $\frac{1}{4} = \frac{2}{8}$  and when  $\frac{2}{8}$  are halved, they make  $\frac{1}{8}$ .  $\frac{1}{4} = \frac{2}{8}$  are equal.

$\frac{1}{16} \leftarrow$  Shape 2: Shape 2 is half of Shape 1.

Answer

$\frac{1}{16}$

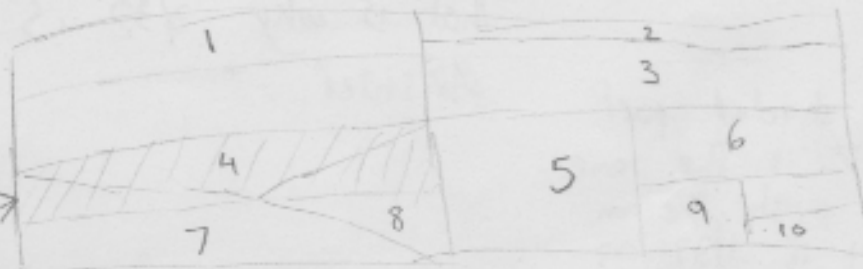
Therefore shape 2 is  $\frac{1}{16}$ . This can be proven by putting two shape 2's in shape 1. Shape two  $\times 2$  doesn't overlap or leave gaps for shape 1.

$\frac{3}{16} \leftarrow$  Shape 3: Shape 1 + Shape 2 = Shape 3.

Shape 1 can be made  $\frac{2}{16}$  and with shape 2

$(\frac{1}{16}) \frac{2}{16} + \frac{1}{16} = \frac{3}{16}$ . Answer

$\frac{1}{16} \leftarrow$  Shape 4:




This is equal to shape 1.

Shape 4 can be halved to make four equal parts. This proves shape 4 is half of the  $\frac{1}{8}$  shape. That means  $\frac{1}{8} \div 2 = \frac{1}{16}$ . Answer

$\frac{1}{8} \leftarrow$  Shape 5: If you cut shape one in half and align them one under another, the shape that is made is shape 5. This means that shape 1 and shape 5 are the same. Hence, since shape 1 is  $\frac{1}{8}$ , that make shape 5 also  $\frac{1}{8}$ .

$\frac{1}{16} \leftarrow$  Shape 6: Shape 6 fits into shape 5 twice perfectly. This means shape 6 is half the size of shape 5. Shape five is  $\frac{1}{8}$  and <sup>can</sup> be turned into  $\frac{2}{16}$  and still be the same value. If you half  $\frac{2}{16}$ , it makes  $\frac{1}{16}$ . Therefore, shape 6 is  $\frac{1}{16}$ .

$\frac{3}{32} \leftarrow$  Shape 7:



The shaded part is the same as shape 4 which is equal to  $\frac{1}{16}$ .  $\frac{1}{16}$  is equal to  $\frac{2}{32}$ . The blank part of shape 7 is half of the shaded part. Thus, being  $\frac{1}{32}$ . The shaded part ( $\frac{2}{32}$ ) + the non shaded part ( $\frac{1}{32}$ ) equals  $\frac{3}{32}$ . That is why  $\frac{3}{32}$  is the answer.

$\frac{1}{32} \leftarrow$  Shape 8: The non shaded part of shape 7 is the same as shape eight. The non shaded part is  $\frac{1}{32}$  as explained before. That is why it is  $\frac{1}{32}$ .

Shape 9: Shape 9 is half of shape shape 6. Since shape 6 is  $1/16$  and can be turned in  $2/32$  (still having the same value). When you half  $2/32$ , it makes  $1/32$ .

Shape 10: Shape 10 is half of shape 9 which is  $1/32$ .  $1/32$  is the same as  $2/64$  and half of  $2/64$  is  $1/64$ . That is why  $1/64$  is the answer.

The big rectangle was divided into 4 main quarters.



To make sure each shape had the right fraction, I added each smaller shape in each quarter to add to  $1/4$ .

Quarter 1:  $1/8 + 1/8 = 2/8$  which is equal to  $1/4$ .

Quarter 2:  $3/16 + 1/16 = 4/16$  which is equal to  $1/4$ .

Quarter 3:  $1/16 = 2/32$ .  $2/32 + 1/32 + 1/32 + 1/32 + 3/32 = 8/32$   
 $8/32$  is equal to  $1/4$ .

Quarter 4:  $1/32 = 2/64$ .  $1/16 = 4/64$ .  $1/8 = 8/64$ .  $2/64 + 4/64 + 8/64 + 1/64 + 1/64$   
 $= 16$   $= 16/64$  which is equal to  $1/4$ .

$1/4 \times 4 = 1$  whole rectangle