

**Correct order of steps:**

- g)  $a+b+c=12$
- c)  $a+b=12-c$
- f) By Pythagoras' Theorem:  $a^2+b^2=c^2$
- a) Squaring both sides:  $a^2+2ab+b^2=144-24c+c^2$
- d) So  $2ab=144-24c$
- h) Dividing by 2:  $ab=72-12c$
- e) Area of the triangle  $=ab/2$
- b) So Area of the triangle  $=36-6c$

**Can you adapt your method, or the method above, to prove that when the perimeter is 30 units, the area is  $225-15c$  square units?**

Perimeter is  $a+b+c=30$   
So rearranging gives  $a+b=30-c$   
Using Pythagoras' Theorem :  $a^2+b^2=c^2$   
Squaring both sides gives :  $a^2+2ab+b^2=900-60c+c^2$   
Therefore  $2ab=900-60c$   
Dividing by 2 results in :  $ab=450-30c$   
Area of triangle  $= ab/2$   
So area =  $450-30c$  all divided by 2  
 $= 225-15c$

**Extension**

**Can you find a general expression for the area of a right angled triangle with hypotenuse c and perimeter p?**

Given :  $p = a+b+c$  ;  $c^2=a^2+b^2$  ;  $A= ab/2$   
 $(a+b)^2=a^2+2ab+b^2$   
 $=(a^2+b^2)+2ab$   
Implementing Pythagoras' Theorem :  $a^2+b^2=c^2$  ,  $(a^2+b^2)$  can be substituted as  $c^2$  therefore giving :  $(a+b)^2= c^2+2ab$   
Area of a triangle  $= ab/2$  , so  $2ab = 4A$  wherein A stands for the area of the triangle  
Substituting  $2ab= 4a$  into  $(a+b)^2= c^2+2ab$  leaves  $(a+b)^2= c^2+4A$   
 $p=a+b+c$  and when c is subtracted from both sides gives  $p-c=a+b$   
Squaring both sides leaves:  $(a+b)^2=(p-c)^2$   
 $(a+b)^2=p^2-2pc+c^2$   
Using the two equations: (a)  $(a+b)^2= c^2+4A$   
and (b)  $(a+b)^2=p^2-2pc+c^2$   
The terms  $(a+b)^2$  and  $c^2$  can be cancelled from both sides resulting in  $p^2-2pc=4A$   
To find A on its own, divide by 4 to give :  $A= (p^2-2pc)/4$   
Further simplification gives  $A= p(p-2c)/4$

