

Area of trapezium = 2x Shaded area

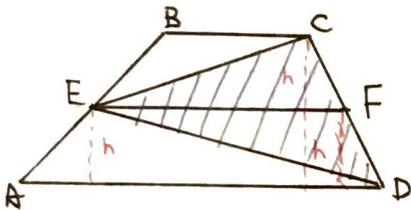
$EF \parallel BC \parallel AD$ E, F is the midpoint of AB, CD
 $\therefore EF = \frac{1}{2}(BC + AD)$

$$\begin{aligned} \text{shaded Area} &= \frac{1}{2} \times EF \times h + \frac{1}{2} EF \times h \\ &= EF \times h \\ &= \frac{1}{2}(BC + AD) \times h \end{aligned}$$

$$\begin{aligned} \text{Area of trapezium} &= \frac{1}{2}(BC + AD) \times 2h \\ &= (BC + AD) \times h \end{aligned}$$

\therefore Area of trapezium = 2x shaded area

Method 1.



make F the midpoint of CD

\therefore E is the midpoint of AB

$\therefore BC \parallel EF \parallel AD$

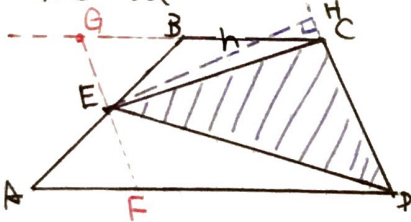
$\therefore EF = \frac{1}{2}(BC + AD)$

$$\begin{aligned} \text{Area of } \triangle CED &= \text{Area of } \triangle CEF + \text{Area of } \triangle DEF \\ &= \frac{1}{2} EF \times h + \frac{1}{2} EF \times h \\ &= EF \times h = \frac{1}{2} h (BC + AD) \end{aligned}$$

$$\text{Area of } ABCD = \frac{1}{2} \times 2h \times (BC + AD) = h(BC + AD)$$

\Rightarrow Area of trapezium = 2x shaded area

Method 2



Extend CB; draw a line through E, parallel to CD, intersect with AD at F and intersect the extension of CB on G with

$\therefore BC \parallel AD$ E is the midpoint

$\therefore \triangle AFE \cong \triangle BGE$

\therefore Area of $\triangle AFE$ = Area of $\triangle BGE$

Area $\triangle AEF$ is now presented as Area $\triangle BEG$

The angle at the midpoint E is moved to the point F

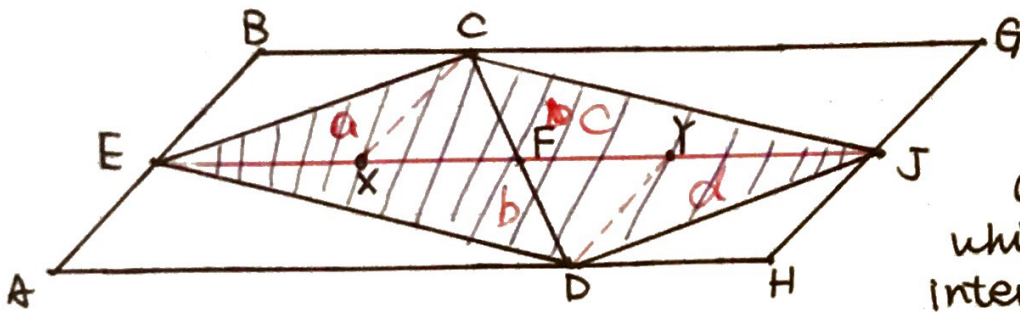
$\therefore FE \parallel HD \therefore EH = FH' = h$

$$\text{Area of shaded area} = \frac{1}{2} h \times CD$$

Area of the parallelogram = $h \times CD$

Area of the parallelogram = area of trapezium
 \therefore area of trapezium = 2x area of shaded area

Method. 3



The two trapeziums forms parallelogram

draw a line through c which is parallel with EB, intersect with EJ at X

draw a line through D, parallel with JH, intersect with EJ at Y

$BG \parallel EJ \parallel AH$ \therefore quadrilateral $BEXC$, $CXJG$, $AEYD$ and $YDHI$ are all parallelograms.

$$S_{\square ABGH} = S_{\square BEXC} + S_{\square CXJG} + S_{\square AEYD} + S_{\square YDHI}$$

$$S_{\square BEXC} = 2S_{\triangle XCE} = 2a \quad S_{\square CXJG} = 2S_{\triangle XCJ} = 2c$$

$$S_{\square AEYD} = 2S_{\triangle EYD} = 2b \quad S_{\square YDHI} = 2S_{\triangle YDJ} = 2d$$

$$\text{Area of } ECJD = a + b + c + d$$

$$\text{Area of } ABGH = 2a + 2b + 2c + 2d$$

$$\therefore \text{Area of } ABGH = 2 \times \text{Area of } ECJD$$

\therefore There are two trapeziums

$$\therefore \text{Area of one trapezium} = a + b + c + d$$

$$\text{Area of shaded area} = \frac{1}{2}(a + b + c + d)$$

$$\therefore \text{Area of trapezium} = 2 \times \text{shaded area}$$