

(c) has a local minimum when $x=1$

$$\frac{dy}{dx} = 0 \quad \text{and} \quad \frac{d^2y}{dx^2} > 0, \quad \text{when } x = -1$$

$$\frac{dy}{dx} = x(x+1) = x^2 + x$$

$x = -1$

$$\int (x^2 + x) dx = \frac{1}{3}x^3 + \frac{1}{2}x^2 + c \Rightarrow y = \frac{1}{3}x^3 + \frac{1}{2}x^2 + c, \quad \text{where } c \text{ is a constant}$$

$$\frac{dy}{dx} = x^2 + x \quad \text{so...} \quad \frac{d^2y}{dx^2} = 2x + 1 \quad \text{when } x = -1 \quad \frac{d^2y}{dx^2} < 0$$

↖ maximum
↑

$$\frac{d^2y}{dx^2} = -2x + 1$$

we want a minimum, so we need to make a change

$$\int (-2x + 1) dx = -x^2 + x$$

$$\int (-x^2 + x) dx = -\frac{1}{3}x^3 + \frac{1}{2}x^2 + c \quad \text{so...} \quad \boxed{y = -\frac{1}{3}x^3 + \frac{1}{2}x^2 + c}$$

$$y = -\frac{1}{3}x^3 - \frac{1}{2}x^2 + 1$$

