

## ANGLES IN THREE SQUARES

- The angle  $c=45^\circ$ , because it is the angle between the diagonal and the side of square.
- I mark points on the diagram, which in essentially to name angles.
- The angle  $\angle CAE$  is  $a$ ,  $\angle BDA$  is  $b$ .
  - The angle  $\angle DCA$  is symmetric with the angle  $\angle CAE$  (alternate angles), so  $\angle DCA = a$ .
  - The angle  $\angle BCD = b$ .
  - The angle  $\angle ABF \cong \angle CBG = b$
  - $\triangle BHC$  is right – angled, so  $\angle CBH = 90^\circ - b$
- $\angle BCA = a+b$   
We have to prove, that  $a + b = c = 45^\circ$
- In  $\triangle ABC$  the line segments  $AB$  and  $BC$  are symmetric.  $AB \cong BC$ , this is why  $\triangle ABC$  is isosceles, so is  $\angle BAC \cong \angle BCA$ .  $\angle BAC = a + b$ .
- The equation for angles in  $\triangle ABC$ :

$$\begin{aligned}
 180^\circ &= \angle ABC + \angle BAC + \angle ACB \\
 180^\circ &= ((90^\circ - b) + b) + (a + b) + (a + b) \\
 180 &= 90^\circ + (a+b) + (a+b) \\
 180^\circ &= 90^\circ + 2 \cdot (a+b) \\
 180^\circ - 90^\circ &= 2 \cdot (a + b) \\
 90^\circ &= 2 \cdot (a + b) \\
 90^\circ : 2 &= a + b \\
 \underline{45^\circ} &= \underline{a + b}
 \end{aligned}$$

The sum of angles  $a$  and  $b$  in  $45^\circ$ . And angle  $c$  is  $45^\circ$  too.  
 $a + b = c$

