

\uparrow 2 3 4^v 5 6 7 8 9
 10 11 12 13 14 15 16 17 18
 1 2 3 4 5 6 7 8 9

$$\underline{10} - 1 = \underline{9}$$

Adding 9 is
 taking 1 off but
 adding 10.

eg. $1 \rightarrow 0 \rightarrow 10$

Basically, we're moving one of the ones
 into the tens.

So, when you add the digits, it becomes the same next

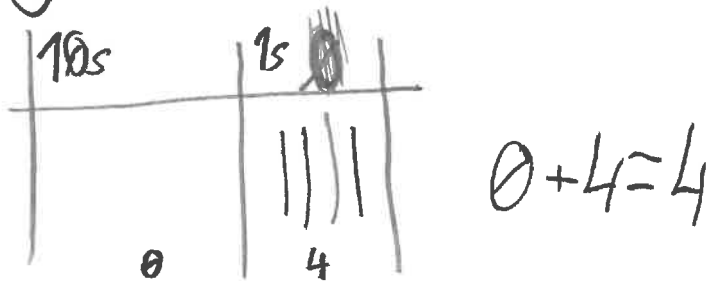
2

$$1 \leq n \leq 9$$

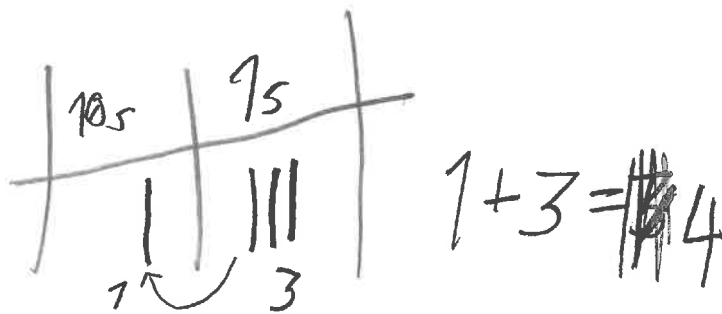
$$\exists x \{x+9 = (x-1) + 10\}$$

for
any
value,

e.g.



+9
↓



What if this was in different bases?

3

base 12

$x=10$
 $\epsilon=7$

~~7~~ + ϵ

1 2 3 4 5 6 7 8 9 x ϵ

We need to add ϵ , not 9 because $9 < x < \epsilon < 10$
So ϵ is the biggest digit

10 11 12 13 14 15 16 17 18 19 1x

1 1 1 1 1

1 2 3 4 5 6 7 8 9 x ϵ

- f
- 1e
- 2d
- 3c
- 4b
- 5a
- 6g
- 87
- 78

4af2

$$\begin{array}{r} x \qquad \qquad c \\ \hline \qquad \qquad \qquad 8 \end{array}$$

4af2

$$\begin{array}{r} x \qquad \qquad 9 \\ \hline 2a, 8, 9, 7 \end{array}$$

16⁷⁰
256
16³
16⁴
H
S
M
L

$$16 \overline{) 80} \quad 5$$

$$16 \overline{) 180} \quad \begin{array}{l} 11 \\ 4 \end{array} \frac{16}{16}$$

$$\begin{array}{r} 180 \\ -16 \\ \hline 20 \end{array}$$

24

$$\begin{array}{r} 16 \\ + 32 \\ \hline 48 \\ 64 \\ 80 \\ 96 \end{array}$$

$$\begin{array}{r} 15 \\ + 12 \\ \hline 27 \\ 75 \\ \hline 780 \end{array}$$