

The Koch Snowflake

Start with This equilateral triangle of length L, area A

Iteration	No. of sides	Length of each side	Total length	No. of small triangles added	Area of each small triangle	Total area added	Total Area	Notes
1	3	L	3L		$\frac{1}{9} \times A$	$3 \times (\frac{1}{9}A)$	A	
2	$3 \times 4 = 12$	$\frac{1}{3} \times L$	$3 \times 4 \times (\frac{1}{3}L)$	3	$\frac{1}{9} \times (\frac{1}{9}A)$ $= (\frac{1}{9})^2 \times A$	$6 \times 2 \times (\frac{1}{9})^2 A$	$A + 3 \times (\frac{1}{9} \times A)$	each side is replaced by a triangle which has 4 sides Refer to Notes *
3	$3 \times 4 \times 4 = 3 \times 4^2 = 48$	$\frac{1}{3} \times (\frac{1}{3} \times L)$ $= \frac{1}{9} \times L$	$3 \times 4^2 \times (\frac{1}{9}) \times L$	6×2	$\frac{1}{9} \times (\frac{1}{9})^2 \times A$ $= (\frac{1}{9})^3 \times A$	$6 \times 2 \times 2 \times (\frac{1}{9})^3 A$ $= 6 \times 2^2 \times (\frac{1}{9})^3 A$	$A + 6 \times 2 \times (\frac{1}{9})^2 A$	
4	$3 \times 4 \times 4 \times 4 = 3 \times 4^3 = 192$	$\frac{1}{3} \times (\frac{1}{3} \times (\frac{1}{3} \times L))$ $= (\frac{1}{9}) \times (\frac{1}{3}) \times L$	$3 \times 4^3 \times (\frac{1}{9}) \times L$	$6 \times 2 \times 2$	$(\frac{1}{9})^4 \times A$	$6 \times 2^3 \times (\frac{1}{9})^4 A$ $= 6 \times 2^{n-2} \times (\frac{1}{9})^{n-1} A$	$A + 6 \times 2^2 \times (\frac{1}{9})^3 A$ $(1 + 6 \times 2^{n-1} \times (\frac{1}{9})^{n-1}) A$	
n	$3 \times 4^{n-1}$	$(\frac{1}{3})^{n-1} \times L$	$3 \times 4^{n-1} \times (\frac{1}{3})^{n-1} \times L$	$6 \times 2^{n-2}$				

NOTES

The small Δ is $\frac{1}{9}$ of the big Δ

ΔABC and ΔDEF are the same

