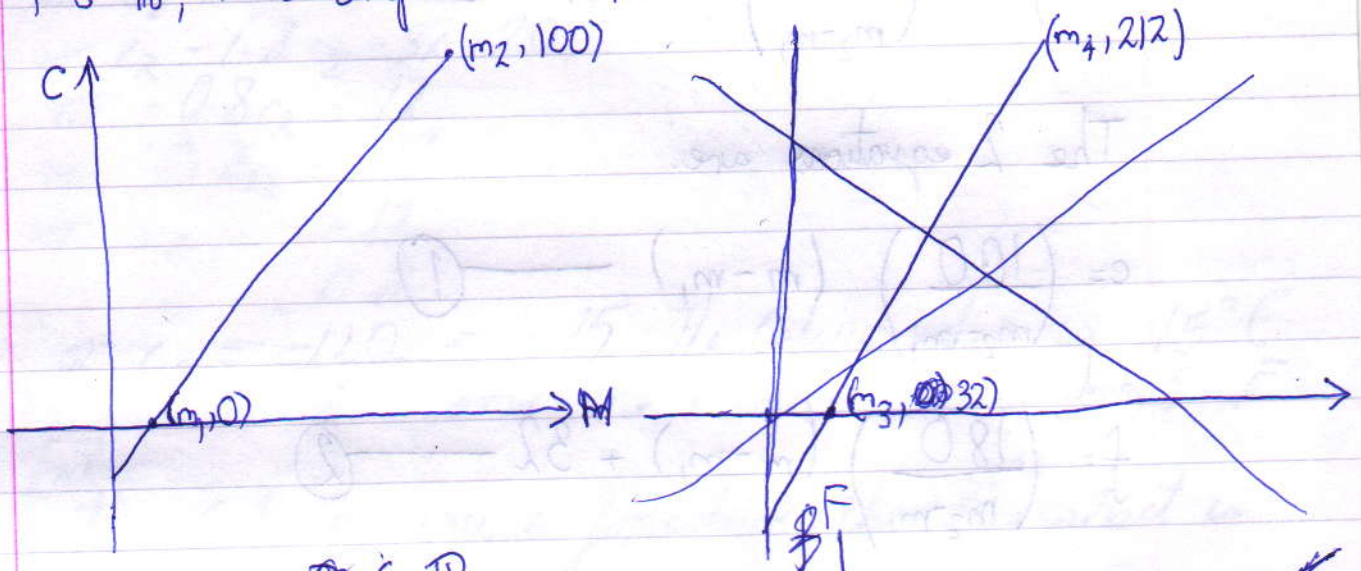


15.5.11, Temperature Niharika Paul / Leicester High School For Girls X4

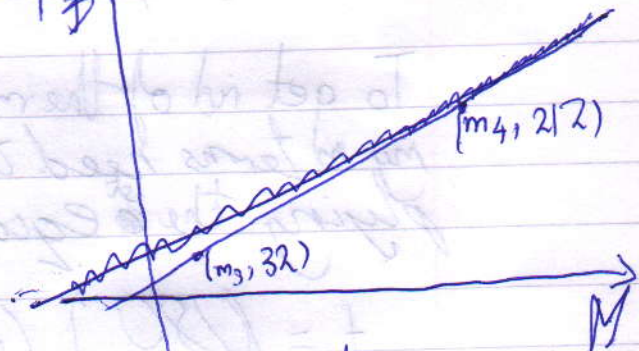
Here, I am using a mercury thermometer

(Here I define my variables)

$M \in \mathbb{R}, M > 0$, M is length of mercury column
 $C \in \mathbb{R}$, C is temperature in $^{\circ}\text{Celsius}$
 $F \in \mathbb{R}$, F is temperature in $^{\circ}\text{Fahrenheit}$



(Here I define my constants)
 $m_1, m_2, m_3, m_4 \in \mathbb{R}$
 m_1 is length of mercury at freezing point of water, $m_1 = m_3$
 m_2 is length of mercury at boiling point of water, $m_2 = m_4$



Using slope of linear function we find C as a function of M .
 I use my points $(m_1, 0)$, $(m_2, 100)$ and a general point (m, c)

$$\therefore \frac{c-0}{m-m_1} = \frac{100-0}{m_2-m_1}$$

$$\text{or } \frac{c}{m-m_1} = \frac{100}{m_2-m_1}$$

$$\text{or } c = \left(\frac{100}{m_2-m_1} \right) (m-m_1)$$

Similarly:

$$\frac{f-32}{m-m_1} = \frac{212-32}{m_2-m_1}$$

$$\text{or } \frac{f-32}{m-m_1} = \frac{180}{m_2-m_1}$$

$$\text{or } f-32 = \left(\frac{180}{m_2-m_1} \right) (m-m_1)$$

$$\text{or } f = \left(\frac{180}{m_2-m_1} \right) (m-m_1) + 32$$

The 2 equations are:

$$c = \left(\frac{100}{m_2-m_1} \right) (m-m_1) \quad \text{--- (1)}$$

and

$$f = \left(\frac{180}{m_2-m_1} \right) (m-m_1) + 32 \quad \text{--- (2)}$$

To get rid of the m terms by doing simple subtraction; m terms need to be equal. We can do this by multiplying the equation by 1.8.

$$f = \left(\frac{180}{m_2-m_1} \right) (m-m_1) + 32$$
$$- [1.8c = \left(\frac{1.8 \times 100}{m_2-m_1} \right) (m-m_1)]$$

$$\text{or } f - 1.8c = 32$$

$$\text{or } f = 32 + 1.8c \quad \text{--- (3)}$$

Let

The value which the temperature, in Celsius and Fahrenheit is the same ^{scales are} as c that is equal

$$\therefore c_1 = 32 + 1.8c_1 \quad (\text{from (3)})$$

$$\text{or } c_1 - 1.8c_1 = 32$$

$$\text{or } -0.8c_1 = 32$$

$$\text{or } 0.8c_1 = -32$$

$$\text{or } c_1 = \frac{-32}{0.8} = -40 \quad \text{Ans}$$

0.8

Let

the Celsius value for which the Fahrenheit is 20° more is c_2

$$\therefore c_2 + 20 = 32 + 1.8c_2 \quad (\text{from (3)})$$

$$\text{or } c_2 + 20 - 1.8c_2 = 32$$

$$\text{or } c_2 - 1.8c_2 = 32 - 20$$

$$\text{or } -0.8c_2 = 12$$

$$\text{or } 0.8c_2 = -12$$

$$\text{or } c_2 = \frac{-12}{0.8}$$

Ans

$$\text{or } c_2 = \frac{-120}{8} = -15 \text{ The Celsius value is } -15^\circ\text{C} \text{ and the Fahrenheit value is } +5^\circ\text{F}$$

Let

the Celsius value for which the Fahrenheit is 20° lower is c_3

$$\therefore c_3 - 20 = 32 + 1.8c_3$$

$$\text{or } c_3 - 20 - 1.8c_3 = 32$$

$$\text{or } c_3 - 1.8c_3 = 32 + 20$$

$$\text{or } -0.8c_3 = 52$$

$$\text{or } 0.8c_3 = -52$$

$$\text{or } c_3 = \frac{-52}{0.8}$$

$$\text{or } c_3 = \frac{-520}{8} = -65 \text{ The Celsius value is } -65^\circ\text{C} \text{ and the Fahrenheit value is } -85^\circ\text{F}$$

Ans

As the gradations for Celsius and Kelvin are the same you simply add or translate

$$K = 273.15 + C \quad \text{--- (4)}$$

We can find the relation between Kelvin and Fahrenheit by using the relation between Fahrenheit and Celsius

~~$f = 32 + 1.8(C + 273.15)$
 $K = 273.15 + K$
 $or K = 273.15$
 This is not possible~~

$f = 32 + 1.8(K - 273.15)$ — (5)

Is there a common temperature on the $^{\circ}C$ and K scales?

$K = 273.15 + K$
 $or K - K = 273.15$

This is not possible (\because the relation is translation) Ans

$f = 32 + 1.8(f - 273.15)$
 $or f = 32 + 1.8f - 491.67$
 $or f - 1.8f = 32 - 491.67$
 $or -0.8f = -459.67$
 $or 0.8f = 459.67$
 $or f = \frac{459.67}{0.8} \approx \frac{4600}{8} = \frac{1150}{2} = 575^{\circ}F$ Ans

Is there a common temperature on the $^{\circ}F$ and K scales?

$\frac{4600}{8} = \frac{1150}{2} = 575^{\circ}F$ Ans