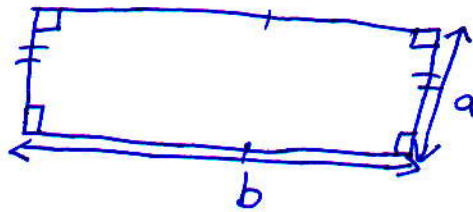


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Can they Be Equal?

Age 9



$A$  is the set of all  $a$ .  
 $B$  is the set of all  $b$ .

I know that:

$$ab = 2a + 2b$$

$$\text{or } b = 2 + \frac{2b}{a}$$

$$\text{or } b - \frac{2b}{a} = 2$$

$$\text{or } \left(\frac{a-2}{a}\right)b = 2$$

$$\text{or } b = \frac{2a}{a-2}$$

I know that  $a, b > 0$

Then  $2a > 0, b > 0$

$$\therefore a - 2 > 0$$

$$\therefore a > 2$$

We use constraints to decrease the no. of ~~eq~~ rectangles.  
In this case we used the fact that  $a, b > 0$ . There are  $\infty$  such rectangles.

Here the rectangles are shown with their area and perimeter, which are functions of  $a, b$ . So if I reduce the numbers of values of  $a, b$  I reduce perimeter and area. I choose 3 different cases for different ordering of  $a, b$ .

Case 1.  $a = b$

~~is~~

$$b = \frac{2b}{b-2}$$

$$\text{or } b(b-2) = 2b$$

$$\text{or } b^2 - 2b = 2b$$

$$\text{or } b^2 = 4b$$

$$\text{or } b = 4$$

~~Case 2.~~  $a > b$

$$b < 4 < a$$

and ~~Case 3.~~  $a < b$

$$b > 4 > a$$

However using this ordering we do double counting. When  $a$  is 6 and  $b$  is 3 is the same as  $a$  is 3,  $b$  is 6. So we can simply say that the shorter side  $< 4$  and longer side  $> 4$ .



The shorter side of the rectangle  $\leq 4$  and the longer side  $\geq 4$ , so  
that shorter side =  $\frac{2 \times \text{longer side}}{\text{longer side} - 2}$ . As there are  $\infty$   
such rectangles Alison is right. The above supports her  
statement.