

## Exploring Cubic Graphs

There are 12 graphs altogether, though they overlap to form 6 pairs which have rather beautiful, symmetrical patterns. Each cubic pair are similar to each other, as they are the negative form of the algebraic graph equation:

In this brief, yet hopefully explanation, I shall state the functions of each of the cubic graph.

Two functions are given to us. They are:

$$y = (x + 6)^3 - 2$$

$$y = -(x - 9)^3 - 3$$

Using an app like Geogebra or Desmos graphing calculator, we know that the graph (f) is the function  $y = (x + 6)^3 - 2$ . Therefore, the ~~graph~~ graph (e) is the negative form of the function (f) which is the equation  $-(x + 6)^3 - 2$ .

The graph (m) is  $-(x - 9)^3 + 3$ . Therefore the graph (n) is  $(x - 9)^3 + 3$ .

Equations of the cubic graphs

$$(k) : y = -(x - 6)^3 + 2$$

$$(l) : y = (x - 6)^3 + 2$$

$$(i) : y = -(x - 3)^3 + 1$$

$$(j) : y = (x - 3)^3 + 1$$

$$(g) : y = -(x - 0)^3 + 0$$

$$(h) : y = (x - 0)^3 + 0$$

$$(e) : y = -(x+3)^3 - 1$$

$$(f) : y = (x+3)^3 - 1$$

$$(c) : y = -(x+6)^3 - 2$$

$$(d) : y = (x+6)^3 - 2$$

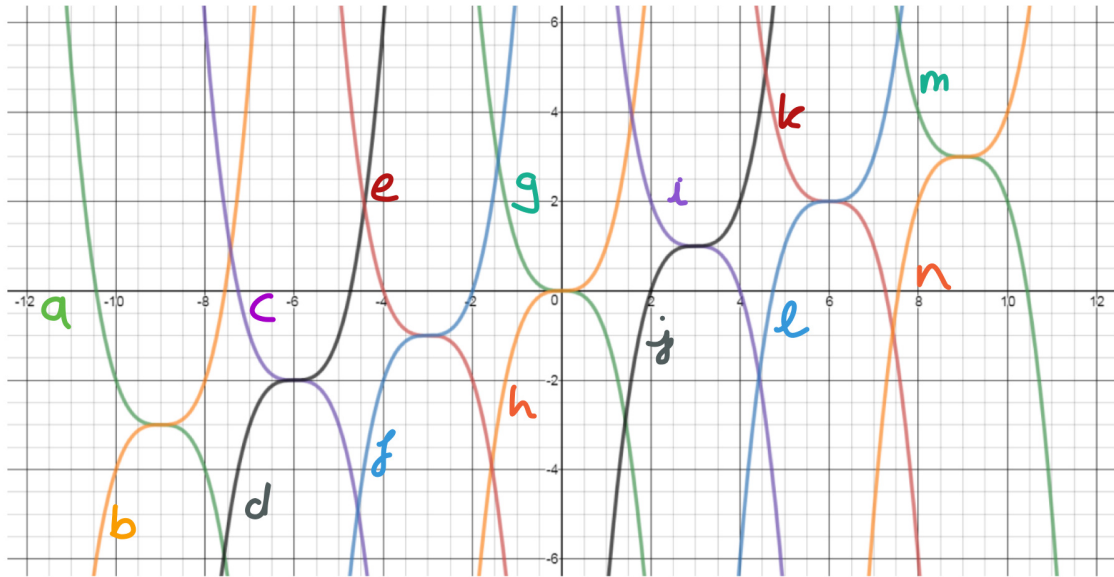
$$(a) : y = -(x+3)^3 - 3$$

$$(b) : y = (x+3)^3 - 3$$

The general formula is  $(x+b)^3 - a$ , where  $a$  and  $b$  are integers.

$a$  is the  $y$  line for example in 'a',  $y = -3$ . The integer 'b' seems to increase (or decrease) as a multiple of 3).

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The cubic graphs arranged by letters. The colour of the letter corresponds to the colour of the graph.